

## 3.9 Differentials

WCID? I can compute the propagated error of measurements using differentials

A. Differential- the amount of error in measurements in applications of mathematics

1. Scientists approximate this error by the symbol  $\Delta V$ , where the blank space is filled by a symbol indicating the quantity measured

Ex:  $\Delta V$  for the error in Volume

2. To find this error...think:

$$dx \left( \frac{dy}{dx} = f'(x) \right) dx$$
$$\begin{array}{ccc} dy = f'(x) dx & & \\ \downarrow & & \downarrow \\ \text{diff} & & \text{diff} \end{array}$$

\*\*We now let  $dy$  be approximately the same as  $\Delta y$

3. Set up the derivative, and then fill in the blanks

Ex: Let  $y = x^2$ . Find  $dy$  when  
 $x = 1$  and  $dx = 0.01$

$$dy = f'(x)dx$$

$$dy = 2x \cdot dx$$

$$dy = 2(1)(.01)$$

$$dy = .02$$

Ex. Let  $y = x^3$ . Find  $dy$  when  
 $x = 4$  and  $dx = 0.02$

$$dy = f'(x)dx$$

$$dy = 3x^2 dx$$

$$dy = 3(4^2)(.02) = .96$$

B. This is also called error propagation

1.  $dx$  can be used to indicate the acceptable amount of error

Ex: The radius of a ball bearing is measured to be 0.07 in., with allowable error of 0.01 in. Find the propagated error in the Volume of the ball bearing.

$$V = \frac{4}{3}\pi r^3$$

$$\begin{aligned}dV &= 4\pi r^2 dr \\ &= 4\pi (0.07)^2 (.01) \\ &= .000196\pi\end{aligned}$$

HW: p. 240 7-10, 11-14, 27-30