

4.1B Particular Solutions

WCID? I can find a particular solution of an antiderivative

A. Evaluate: $\int 2x dx = \cancel{x^2} + C$

**this is called the general solution

1. Particular Solution- a solution for a specific instance
2. Given a value for x and $f(x)$, you will now find C

Examples:

Evaluate $\int 2x dx$, where $F(2)=5$

$$\begin{aligned} x^2 + C &\rightarrow f(x) = x^2 + 1 \\ (2)^2 + C &= 5 \quad C=1 \end{aligned}$$

Evaluate $\int \frac{1}{x^2} dx$, where $F(1)=0$

$$\begin{aligned} \int x^{-2} dx &\rightarrow -\frac{1}{x} + 1 \\ -\frac{1}{1} + C &= -1 + C = 0 \\ -1 + C &= 0 \\ C &= 1 \end{aligned}$$

If $f'(x) = \cos x$, find $f(x)$ if $F(\pi)=2$

$$\begin{aligned} \int \cos x dx &= \sin x + C \rightarrow \sin x + 2 = f(x) \\ &= \sin(\pi) + C = 2 \\ &\Rightarrow C = 2 \end{aligned}$$

If $f'(x) = 2x + 3$, find $f(x)$ if $F(-3) = 5$

$$\begin{aligned} \int 2x + 3 \, dx &= x^2 + 3x + C \\ x^2 + 3x + C & \quad (-3)^2 + 3(-3) + C = 5 \\ x^2 + 3x + 5 & \quad 9 - 9 + C = 5 \\ & \quad C = 5 \end{aligned}$$

B. Similar to second derivatives, we can do antiderivatives twice

1. These are applications of particular solutions

Examples

If $f''(x) = 30x$, find $f(x)$ if $f(1) = 1$ and

$$f'(2) = 55$$

$$\begin{aligned} \int 30x \, dx &= 15x^2 + C \\ 15x^2 + C & \quad \text{blue} \\ 15(2)^2 + C = 55 & \quad \text{blue} \\ C = 5 & \quad \text{blue} \end{aligned}$$

$\int 15x^2 - 5 \, dx$
 $5x^3 - 5x + C$
 $5(1)^3 - 5(1) + C = 1$
 $C = 1$

$5x^3 - 5x + 1$

If $f''(x)=4$, find $f(x)$ if $f(2)=14$ and
 $f'(1)=8$

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